

# Buffers:

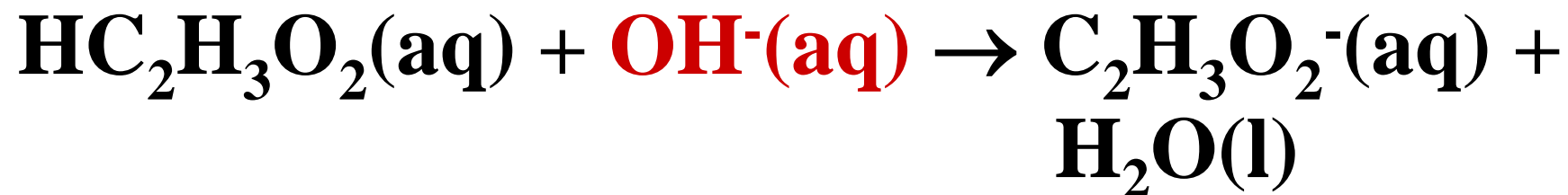


# Buffers:

A buffer is an aqueous system that allows only small changes in pH on the addition of acids or bases.

Consider a system consisting of equal amounts of  $\text{HC}_2\text{H}_3\text{O}_2$  and  $\text{C}_2\text{H}_3\text{O}_2^-$ .

If strong base added:



If strong acid added:



# Identifying Buffers:

**Buffers consist of a weak acid and its corresponding conjugate base.**

**Ex: Is the system  $\text{NH}_3/\text{NH}_4\text{Cl}$  a buffer?**

**Ex: Is the system  $\text{HCl}/\text{Cl}^-$  a buffer?**

# Calculating the pH of Buffer Systems:

**Ex:**

**Calculate the pH of a buffer consisting of 1 M  $\text{NH}_3$  and 1 M  $\text{NH}_4\text{Cl}$ .**

$$\mathbf{K_B = 1.8 \times 10^{-5}}$$

**Answer: pH = 9.26**

**Can use  $K_A$  or  $K_B$  to determine pH.**

**DIFFICULT!!!**

# Henderson-Hasselbalch Equation:

$$\text{pH} = \text{pK}_A + \text{Log} \frac{[\text{base}]}{[\text{acid}]}$$

$$\text{pH} = \text{pK}_A + \text{Log} \frac{\text{moles of base}}{\text{moles of acid}}$$

**Consider a buffer consisting of the weak acid HA and its conjugate base A<sup>-</sup>.**

$$\text{pH} = \text{pK}_A + \text{Log} \frac{[\text{A}^-]}{[\text{HA}]}$$

**Where  $\text{pK}_A = -\text{Log}(\text{K}_A)$**

## Buffer Examples cont...

**Ex:2**

**What is the pH of a buffer prepared by dissolving 25.5 g of  $\text{NaC}_2\text{H}_3\text{O}_2$  in 0.550 M  $\text{HC}_2\text{H}_3\text{O}_2(\text{aq})$  to prepare a 500.0 mL buffer?**

$$\mathbf{K_A = 1.8 \times 10^{-5}}$$

**Ex:3**

**What mass of  $\text{NaC}_2\text{H}_3\text{O}_2$  must be dissolved in 300.0 mL of 0.250 M  $\text{HC}_2\text{H}_3\text{O}_2$  to prepare a buffer of  $\text{pH} = 5.09$ ?**

# Buffer Examples cont...

**Ex:4**

**What is the effect of adding 0.025 moles of HCl to 500.0 mL of a buffer consisting of 0.100 M HC<sub>2</sub>H<sub>3</sub>O<sub>2</sub> and 0.100 M NaC<sub>2</sub>H<sub>3</sub>O<sub>2</sub>?**

$$\mathbf{K_A = 1.8 \times 10^{-5}}$$

**HCl: STRONG ACID**



**Buffer:  $\text{HC}_2\text{H}_3\text{O}_2$  and  $\text{C}_2\text{H}_3\text{O}_2^-$**

**NOTE:  $0.500 \text{ L} \times 0.100 \text{ M} = 0.0500 \text{ mol}$**

<b>From HCl</b>	<b>Buffer base</b>	<b>Buffer Acid</b>
<b><math>\text{H}^+</math></b>	<b><math>\text{C}_2\text{H}_3\text{O}_2^-</math></b>	<b><math>\text{HC}_2\text{H}_3\text{O}_2</math></b>
<b>I: <math>0.025 \text{ mol}</math></b>	<b><math>0.0500 \text{ mol}</math></b>	<b><math>0.0500 \text{ mol}</math></b>
<b>C: <math>-0.025 \text{ mol}</math></b>	<b><math>-0.025 \text{ mol}</math></b>	<b><math>+0.025 \text{ mol}</math></b>
<b>E: <math>0</math></b>	<b><math>0.0250 \text{ mol}</math></b>	<b><math>0.0750 \text{ mol}</math></b>

**NOTE:  $\text{H}^+$  from HCl completely neutralized!!**  
**Only buffer left.**

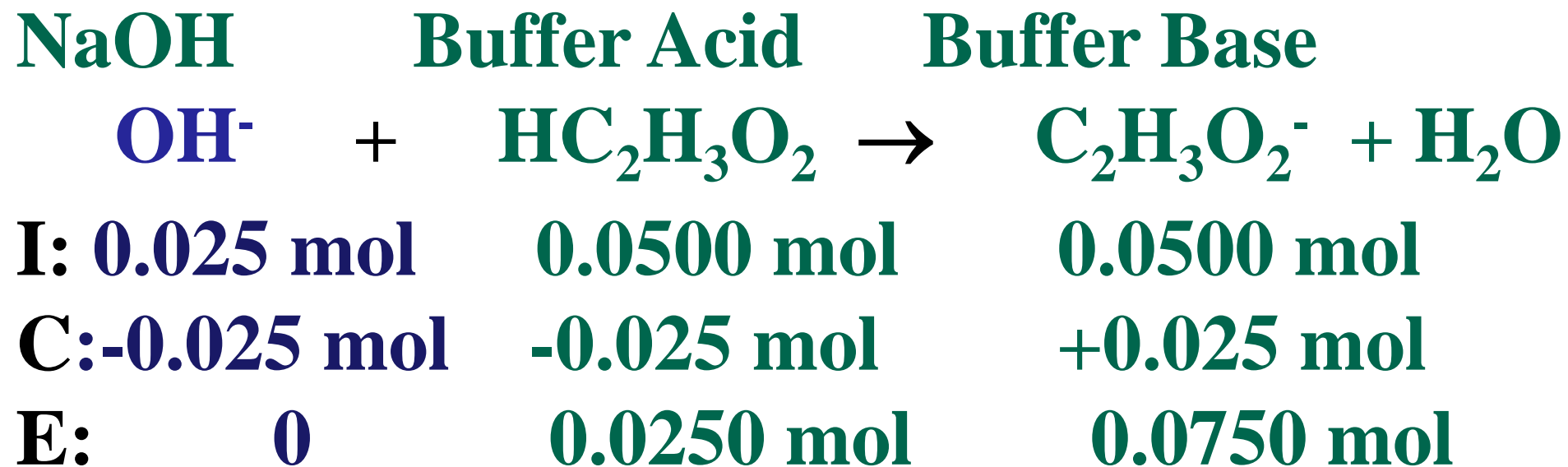


## Ex:5

What is the effect of adding 0.025 moles of NaOH to 500.0 mL of a buffer consisting of 0.100 M HC<sub>2</sub>H<sub>3</sub>O<sub>2</sub> and 0.100 M NaC<sub>2</sub>H<sub>3</sub>O<sub>2</sub>?

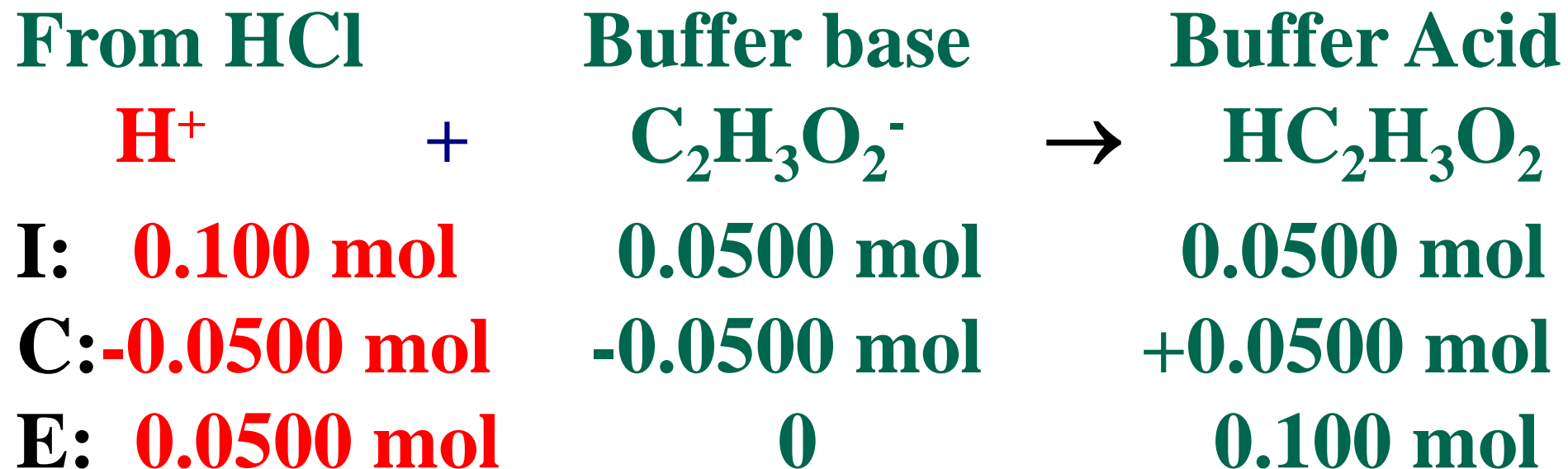
$$K_A = 1.8 \times 10^{-5}$$

From



## Ex:6

What is the effect of adding 0.100 moles of HCl to 500.0 mL of a buffer consisting of 0.100 M  $\text{HC}_2\text{H}_3\text{O}_2$  and 0.100 M  $\text{NaC}_2\text{H}_3\text{O}_2$

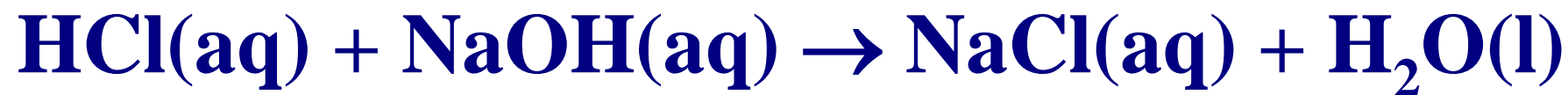


**NOTE: Buffer capacity exceeded!!**

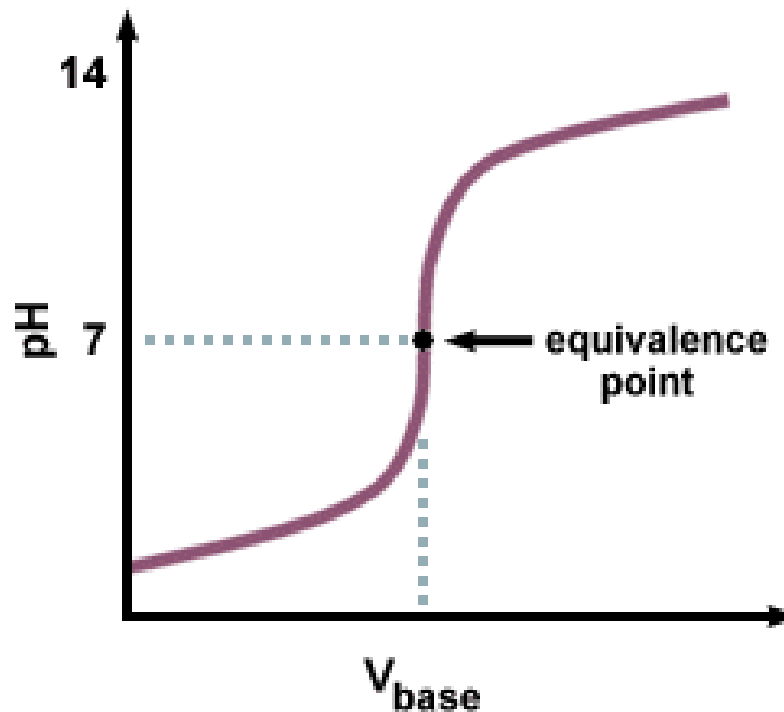
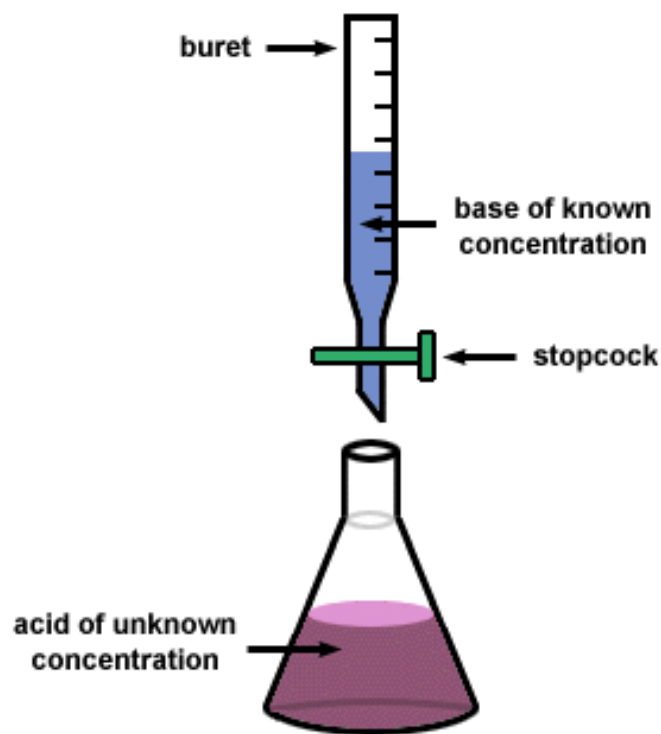
# Acid-Base Titrations:

Types:

Strong Acid/Strong Base

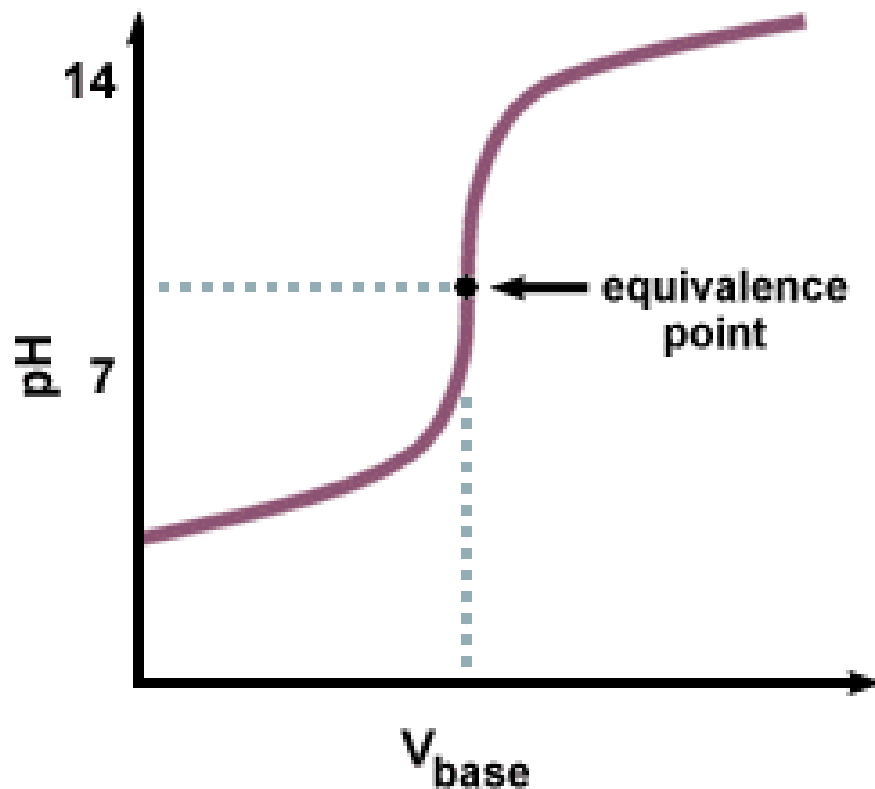


**? M**      **KNOWN M**



# Acid-Base Titrations cont...:

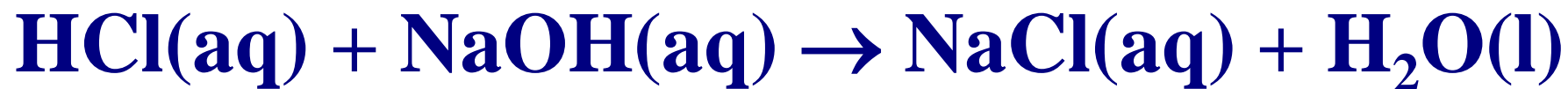
## Weak Acid/Strong Base



# Predicting the pH of an Acid-Base

## Mixture:

**Strong Base – Strong Acid**



**Ex:**

**Consider the titration of 25.0 mL of 1.00 M HCl with 1.00 M NaOH. Calculate the pH on the addition of 10.0 mL, 25.0 mL, and 40.0 mL of the NaOH solution.**

# Ex: Strong Base – Strong Acid:

10.0 mL of 1.00 M NaOH:



<b>I</b>	<b>0.0250 mol</b>	<b>0.0100 mol</b>	<b>0</b>	<b>-</b>
<b>C</b>	<b>-0.0100 mol</b>	<b>-0.0100 mol</b>	<b>+0.0100 mol</b>	<b>+0.0100 mol</b>
<b>F</b>	<b>0.0150 mol</b>	<b>0</b>	<b>0.0100 mol</b>	<b>0.0100 mol</b>

**[HCl] = 0.0150 mol/0.0350 L = 0.429 M**

**Thus pH = 0.368**

# Ex: Strong Base – Strong Acid:

25.0 mL of 1.00 M NaOH:



<b>I</b>	<b>0.0250 mol</b>	<b>0.0250 mol</b>	<b>0</b>	<b>-</b>
<b>C</b>	<b>-0.0250 mol</b>	<b>-0.0250 mol</b>	<b>+0.0250 mol</b>	<b>+0.0250 mol</b>
<b>F</b>	<b>0</b>	<b>0</b>	<b>0.0250 mol</b>	<b>0.0250 mol</b>

**Equivalence point. Only salt water present.**

**Thus pH = 7**

# Ex: Strong Base – Strong Acid:

40.0 mL of 1.00 M NaOH:



<b>I</b>	<b>0.0250 mol</b>	<b>0.0400 mol</b>	<b>0</b>	<b>-</b>
<b>C</b>	<b>-0.0250 mol</b>	<b>-0.0250 mol</b>	<b>+0.0250 mol</b>	<b>+0.0250 mol</b>
<b>F</b>	<b>0</b>	<b>0.0150 mol</b>	<b>0.0250 mol</b>	<b>0.0250 mol</b>

**[NaOH] = 0.0150 mol/0.0650 L = 0.231 M**

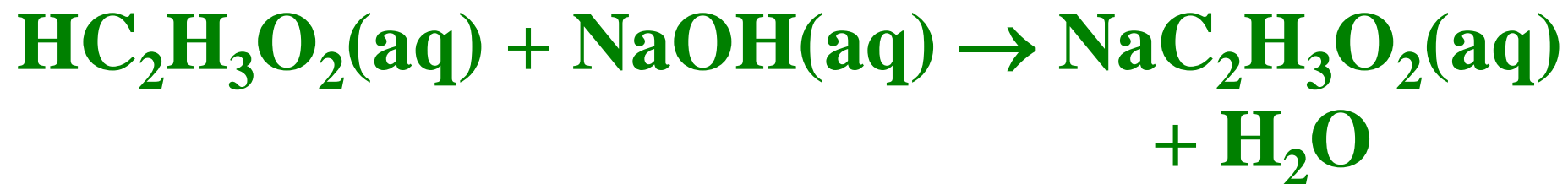
**Thus pH = 13.4**



# Predicting the pH of an Acid-Base

## Mixture:

### Strong Base – Weak Acid



Consider the titration of 25.0 mL of 1.00 M  $\text{HC}_2\text{H}_3\text{O}_2$  with 1.00 M NaOH. Calculate the pH on the addition of 10.0 mL, 25.0 mL, and 40.0 mL of the NaOH solution.

# Ex: Strong Base – Weak Acid:

10.0 mL of 1.00 M NaOH:



<b>I</b>	<b>0.0250 mol</b>	<b>0.0100 mol</b>	<b>0</b>	<b>-</b>
<b>C</b>	<b>-0.0100 mol</b>	<b>-0.0100 mol</b>	<b>+0.0100 mol</b>	<b>+0.0100 mol</b>
<b>F</b>	<b>0.0150 mol</b>	<b>0</b>	<b>0.0100 mol</b>	<b>0.0100 mol</b>

**System a Buffer!!**

**Thus pH = 4.56**

# Ex: Strong Base – Weak Acid:

25.0 mL of 1.00 M NaOH:



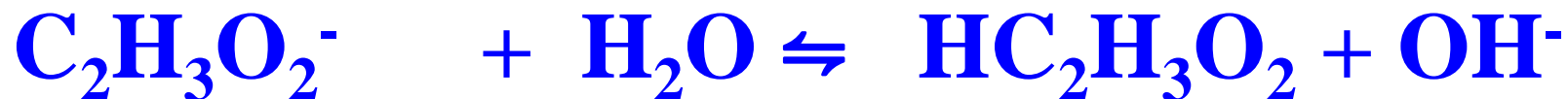
<b>I</b>	<b>0.0250 mol</b>	<b>0.0250 mol</b>	<b>0</b>	<b>-</b>
<b>C</b>	<b>-0.0250 mol</b>	<b>-0.0250 mol</b>	<b>+0.0250 mol</b>	<b>+0.0250 mol</b>
<b>F</b>	<b>0</b>	<b>0</b>	<b>0.0250 mol</b>	<b>0.0250 mol</b>

**System only contains a weak base and water.  
pH determined by weak base.**

# Ex: Strong Base – Weak Acid

cont...:

$$[\text{C}_2\text{H}_3\text{O}_2^-] = 0.0250 \text{ mol}/0.0500 \text{ L} = 0.500 \text{ M}$$



<b>I</b>	<b>0.500 M</b>	<b>-</b>	<b>0</b>	<b>-</b>
<b>C</b>	<b>-X</b>		<b>+X</b>	<b>+X</b>
<b>E</b>	<b>0.500-X</b>		<b>X</b>	<b>X</b>

$$K_B = 5.56 \times 10^{-10} = \frac{X \cdot X}{0.500 - X}$$

$$X = [\text{OH}^-] = 1.67 \times 10^{-5} \text{ M, thus pH} = 9.22$$

# Ex: Strong Base – Weak Acid:

40.0 mL of 1.00 M NaOH:



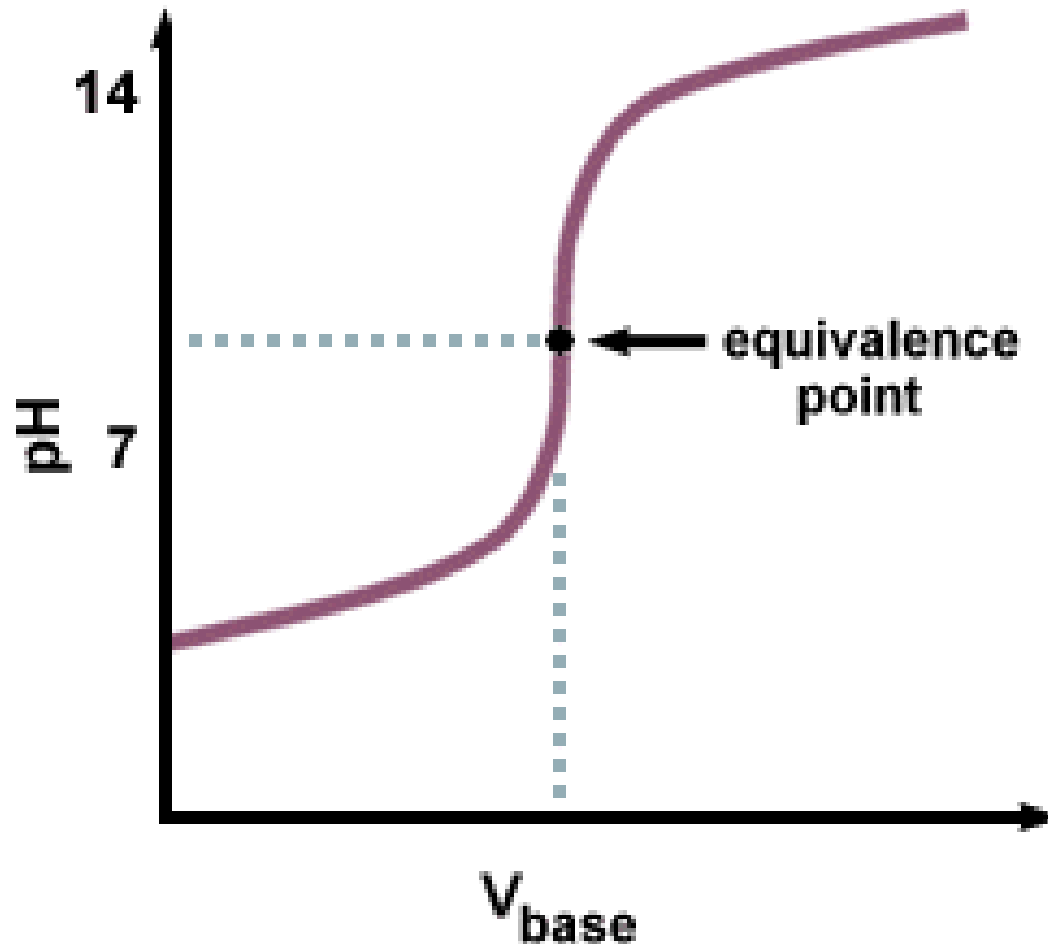
<b>I</b>	<b>0.0250 mol</b>	<b>0.0400 mol</b>	<b>0</b>	<b>-</b>
<b>C</b>	<b>-0.0250 mol</b>	<b>-0.0250 mol</b>	<b>+0.0250 mol</b>	<b>+0.0250 mol</b>
<b>F</b>	<b>0</b>	<b>0.0150 mol</b>	<b>0.0250 mol</b>	<b>0.0250 mol</b>

**[NaOH] = 0.0150 mol/0.0650 L = 0.231 M**

**Thus pH = 13.4**

# Acid-Base Indicators:

During acid base titration pH changes abruptly at equivalence point.

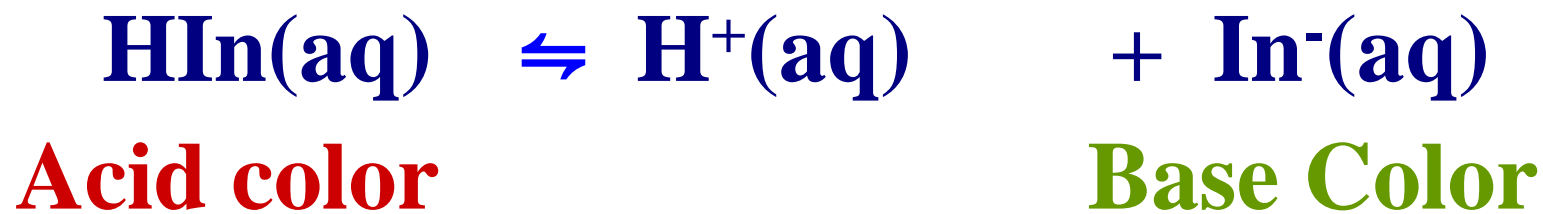


# Acid-Base Indicators:

An acid base indicator is a weak acid whose color depends on the pH of the solution.

**HIn: weak acid(acid color)**

**In<sup>-</sup>: conjugate base(basic color)**



# Acid-Base Indicators cont...:

$$\text{pH} = \text{p}K_{\text{HIn}} + \text{Log} \frac{[\text{In}^-]}{[\text{HIn}]}$$

$$\frac{[\text{In}^-]}{[\text{HIn}]} > 10$$

**Base Color**

$$\frac{[\text{In}^-]}{[\text{HIn}]} < 0.1$$

**Acid color**



## Some Indicators:

<b>Indicator</b>	<b>Acid Color</b>	<b>Base Color</b>	<b>pH Range</b>
<b>phenolphthalien</b>	<b>clear</b>	<b>red</b>	<b>8-10</b>
<b>bromophenol blue</b>	<b>yellw</b>	<b>blue</b>	<b>3-4.5</b>
<b>Methyl Orange</b>	<b>red</b>	<b>yellw</b>	<b>3-5</b>

**Ex:**

**The indicator methyl red has a  $pK_{HI_n}$  of 4.95. If the indicator is placed in a solution with a  $pH = 4.74$ , is it in the acid or base form?**

# Solubility Equilibria:

Solubility equilibria centres on the study of heterogeneous systems.

An aqueous solution containing aqueous NaCl and solid NaCl contains the following equilibrium.

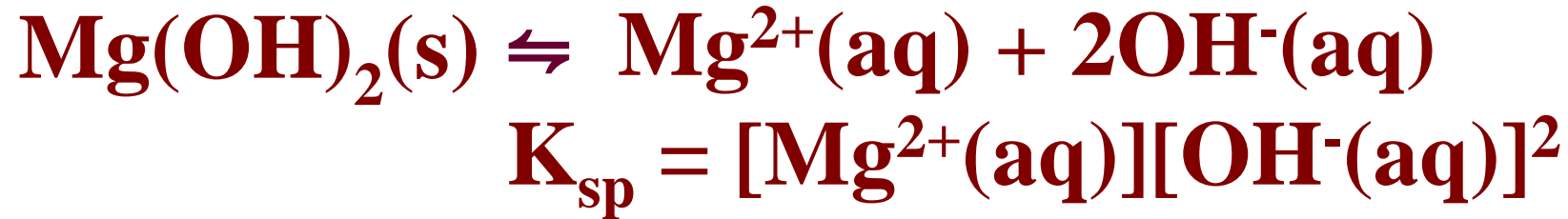


$$K_{\text{sp}} = [\text{Na}^{\text{+}}(\text{aq})][\text{Cl}^{-}(\text{aq})]$$

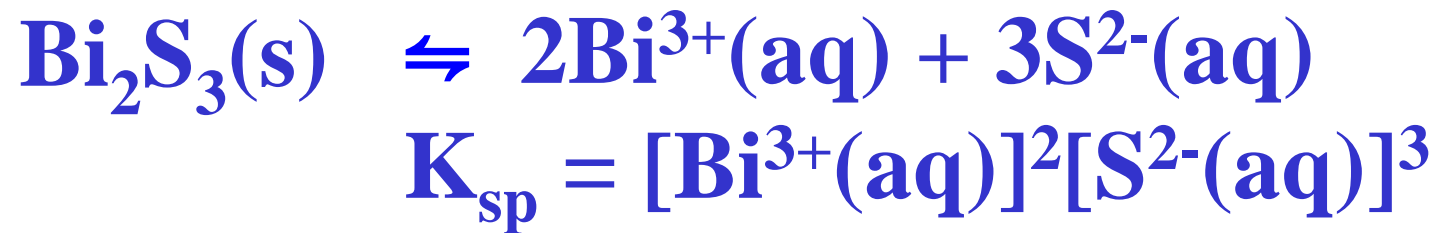
This equilibrium is described by the equilibrium constant,  $K_{\text{sp}}$  (solubility product).

# Examples:

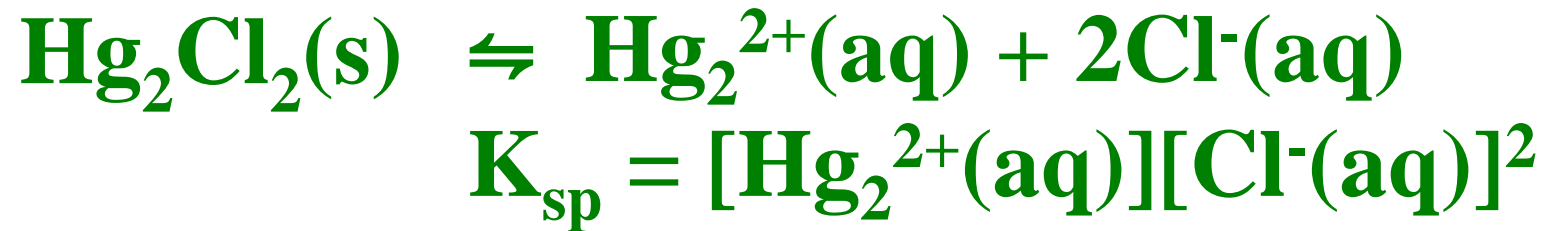
**Ex:**



**Ex:2**



**Ex:3**



# **K<sub>sp</sub> and Solubility:**

**solubility – Concentration of a saturated solution.**

**Denoted by “s”.**

**If we know the solubility we can calculate K<sub>sp</sub> and likewise given K<sub>sp</sub> we can calculate the solubility.**

**Examples:**

**Ex:**

**Silver chloride has a solubility of  $1.31 \times 10^{-5}$  M.  
Calculate  $K_{sp}$ .**

**Ex:2**

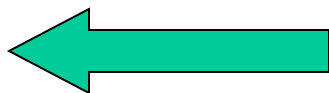
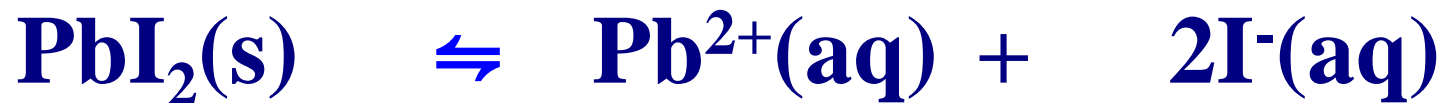
**Calculate the solubility of  $PbI_2$ .**

$$K_{sp} = 7.1 \times 10^{-9}$$

# Common-Ion Effect and Solubility

The solubility of a slightly soluble solute is decreased in the presence of a common ion.

Consider  $\text{PbI}_2$  in the presence of  $\text{KI}$ .



$\text{PbI}_2$  ppt  
out

$[\text{Pb}^{2+}(\text{aq})]$   
decreases

$[\text{I}^{-}(\text{aq})]$  is  
greater

**Examples:**

**Ex:3**

**What is the solubility of  $\text{PbI}_2$  in 0.10 M KI?**

$$\mathbf{K_{sp} = 7.1 \times 10^{-9}}$$

# Reaction Quotient(Q):

Used to determine if a solution is dilute, saturated, or supersaturated.

$$Q = K_{sp} \quad \text{saturated}$$

$$Q < K_{sp} \quad \text{unsaturated}$$

$$Q > K_{sp} \quad \text{supersaturated} \\ \text{(ppt occurs)}$$



# Reaction Quotient(Q) cont...:

**Ex:**

**If  $\text{AgNO}_3$  and  $\text{KI}$  are mixed to obtain a solution with  $[\text{Ag}^+(\text{aq})] = 0.010 \text{ M}$  and  $[\text{I}^-(\text{aq})] = 0.015 \text{ M}$ , is the solution unsaturated, saturated, or supersaturated?**

$$\mathbf{K_{sp}(\text{AgI}) = 8.5 \times 10^{-17}}$$